FINDING THE MINIMUM SEMI-DEFINITE RANK OF A GRAPH

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A matrix $A \in M_n(\mathbb{C})$ is called *Hermitian* if $A = A^*$. A Hermitian matrix with nonnegative eigenvalues is called a *positive semi-definite (PSD)* matrix. Given a Hermitian matrix A we associate a simple, undirected graph G with vertices $V(G) = \{1, \cdots, n\}$ and edges $E(G) = \{(i, j) \mid a_{ij} \neq 0, i \neq j\}$. This associated graph is independent of the diagonal entries of A. Given a graph G, the *minimum semi-definite rank* of G, denoted $msr(G)$, is the minimum of rank of A as A varies over all PSD matrices with graph G.

In this talk we present results on the upper and lower bounds for $msr(G)$, and the effect of topological changes such as vertex or edge modifications on $msr(G)$. In addition, we will discuss the $msr(G)$ for some classes of graphs, including bipartite graphs and chordal graphs.

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